

Electronic states

Each electron has a unique set of quantum numbers (Pauli Exclusion Principle)

- n principle (<u>1</u>s, <u>2</u>s, <u>3</u>s,...)
- I angular momentum (I =0=s, I=1=p)
- m magnetic
- s spin

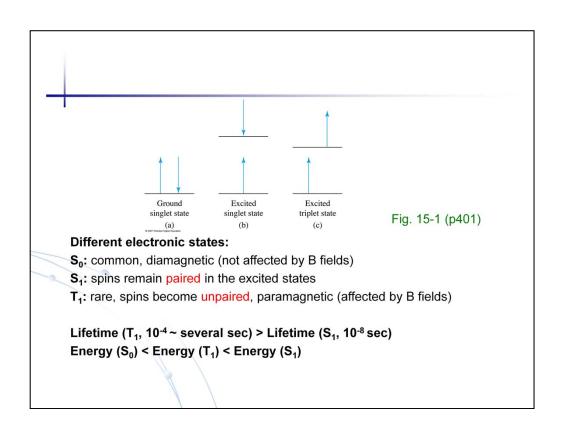
Any two electrons in same orbital (n,l,m) must have different spins

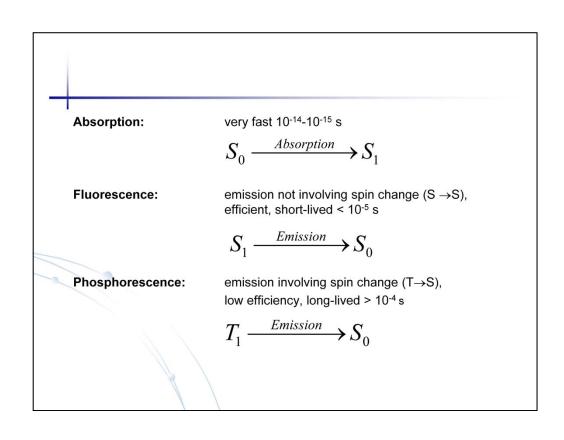
$$s = +\frac{1}{2} \text{ or } -\frac{1}{2}$$

$$S = |\Sigma s_i|$$

Multiplicity

2S+1 (1 = singlet sate, 2 = doublet state, 3 = triplet state, ...)





- Internal conversion: intermolecular radiationless transition to a lower electronic state where vibrational energy levels "overlaps" in energy
- External conversion: radiationless transition to a lower state by collisions between the excited state and solvent or other solute
 - solvent effects on fluorescence
- Intersystem crossing: transition with spin change (e.g. S → T)
 - common in molecules containing heavy atoms
- *Predissociation: relaxation to a lower electronic state with enough vibrational energy to break a bond
 - mostly affected by structure
- *Dissociation: excitation to a vibrational state with enough energy to break a bond

2 Molecular Absorption and Beer's Law

2.1 Excitation of outer valence (bonding) electrons

$$M + h\nu \xrightarrow{excitation} M*$$

Absorbing species

Organic molecules

 σ , π (bonding), n(non-bonding), σ^* , π^* (anti-bonding) orbitals

$$\sigma \rightarrow \sigma^*$$
 large ΔE (λ < 150 nm, out of range)
 ϵ = 10 -10,000 Lmol⁻¹cm⁻¹

$$n \rightarrow \sigma^*$$
 smaller ΔE (λ = 150 - 250 nm)
 ϵ = 200-2000 Lmol⁻¹cm⁻¹

 $\pi \to \pi^*$

 $n \to \pi^*$ smallest ΔE smallest

 $(\lambda = 200 - 700 \text{ nm})$

 $\epsilon = 10\text{-}10,000 \text{ Lmol}\text{-}^{1}\text{cm}\text{-}^{1}$ Ideal for UV-Vis spectrometry of organic chromophore

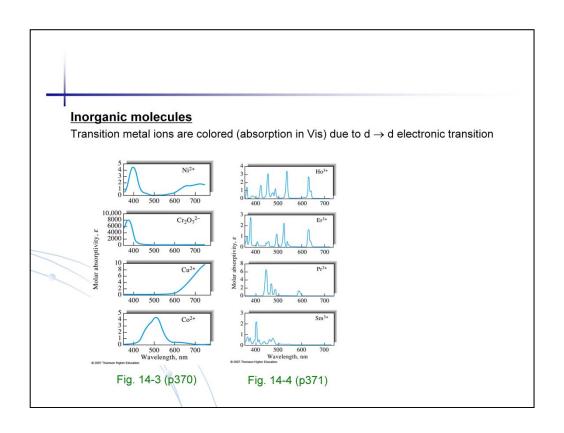
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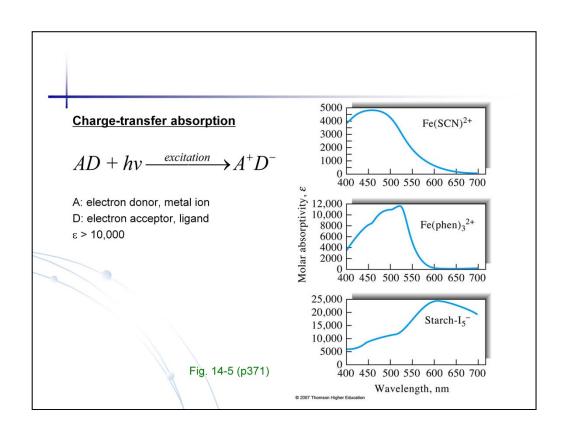
Antibonding

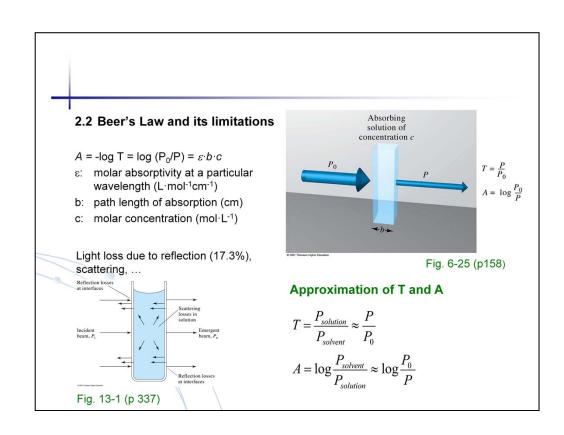
TABLE 14-1 Absorption Characteristics of Some Common Chromophores

Chromophore	Example	Solvent	λ_{\max} , nm	$\varepsilon_{\mathrm{max}}$	Transition Type
Alkene	$C_6H_{13}CH=CH_2$	n-Heptane	177	13,000	$\pi \to \pi^*$
Alkyne	$C_5H_{11}C \equiv C - CH_3$	n-Heptane	178	10,000	$\pi \to \pi^*$
			196	2000	_
			225	160	_
Carbonyl	CH₃ÇCH₃	n-Hexane	186	1000	$n \rightarrow \sigma^*$
	0		280	16	$n \rightarrow \pi^*$
	CH₃CH	n-Hexane	180	large	$n \rightarrow \sigma^*$
	O		293	12	$n \to \pi^+$
Carboxyl	CH ₃ COOH	Ethanol	204	41	$n \rightarrow \pi^*$
Amido	CH₃CNH₂ O	Water	214	60	$n \! \to \! \pi^*$
Azo	CH ₃ N=NCH ₃	Ethanol	339	5	$n \rightarrow \pi^*$
Nitro	CH ₃ NO ₂	Isooctane	280	22	$n \rightarrow \pi^*$
Nitroso	C_4H_9NO	Ethyl ether	300	100	-
			665	20	$n \rightarrow \pi^*$
Nitrate	C ₂ H ₅ ONO ₂	Dioxane	270	12	$n \rightarrow \pi^*$

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Application of Beer's law to mixtures

Absorbance is additive

$$\begin{aligned} \mathsf{A}_{\mathsf{total}} &&= \mathsf{A}_1 + \mathsf{A}_2 + \dots \\ &&= \epsilon_1 \mathsf{bc}_1 + \epsilon_2 \mathsf{bc}_2 + \dots \end{aligned}$$

For a 2-component mixture, we measure the absorption at two different wavelength

$$\mathsf{A}_{\lambda 1} = \varepsilon_{1,\lambda 1} {\cdot} \mathsf{b} {\cdot} \mathsf{c}_1 + \varepsilon_{2,\lambda 1} {\cdot} \mathsf{b} {\cdot} \mathsf{c}_2$$

$$A_{\lambda 2} = \varepsilon_{1,\lambda 2} \cdot b \cdot c_1 + \varepsilon_{2,\lambda 2} \cdot b \cdot c_2$$

2.2.1 Limitations of Beer's Law

Real deviations

At low concentration

$$A = -\log \mathsf{T} = \log \left(\mathsf{P}_0/\mathsf{P}\right) = \varepsilon \cdot b \cdot c$$

At c > 0.01 M

solute-solute interaction, hydrogen bond, ... can alter the electronic absorption of molecules → dilute the solution to remedy problems

 Chemical effects – analyte associates, dissociates or reacts with a solvent to produce different species

Example: Acid-base equilibrium of an indicator

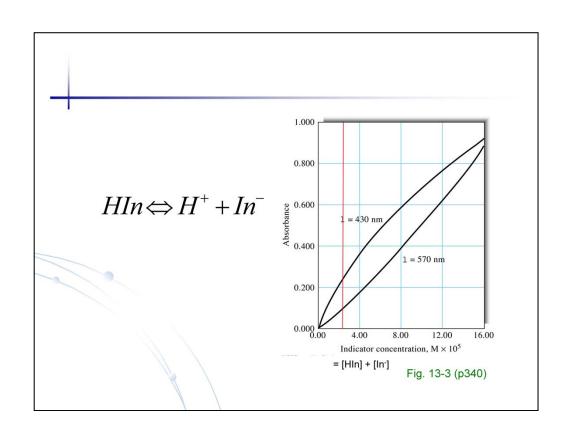
What's the absorbance of unbuffered solution at $c = 2 \times 10^{-5} M$?

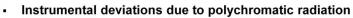
$$K_{a} = \frac{[H^{+}][In^{-}]}{[HIn]} = 1.42 \times 10^{-5} \qquad [In^{-}] = 1.12 \times 10^{-5} M$$

$$[HIn] = 0.88 \times 10^{-5} M$$

$$[H^{+}] = [In^{-}] \qquad A_{430} = \varepsilon_{In^{-},430} b[In^{-}] + \varepsilon_{HIn,430} b[HIn] = 0.236$$

$$A_{570} = \varepsilon_{In^{-},570} b[In^{-}] + \varepsilon_{HIn,570} b[HIn] = 0.073$$





Beer's law applies to monochromatic absorption only.

If a band of radiation consists of two wavelength λ' and $\lambda'',$ Beer's law applies to each wavelength

For first wavelength λ

A'=
$$\log \frac{P_0'}{P'} = \varepsilon' bc$$

P'= $P_0' 10^{-\varepsilon' bc}$

$$P' = P' \cdot 10^{-\varepsilon'bc}$$

For the second wavelength λ'' $P'' = P_0^{''} 10^{-\varepsilon''bc}$

$$P'' = P_0'' 10^{-\varepsilon''bc}$$

Measured absorbance

$$A_{m} = \log \frac{P_{0}^{'} + P_{0}^{"}}{P' + P''} = \log \frac{P_{0}^{'} + P_{0}^{"}}{P_{0}^{'} 10^{-\varepsilon''bc} + P_{0}^{"} 10^{-\varepsilon''bc}}$$

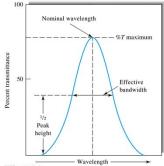
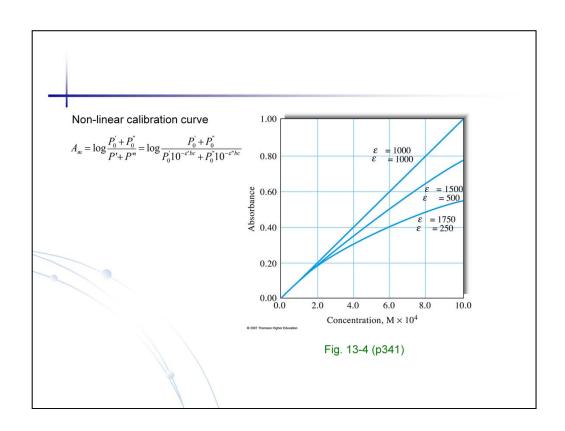
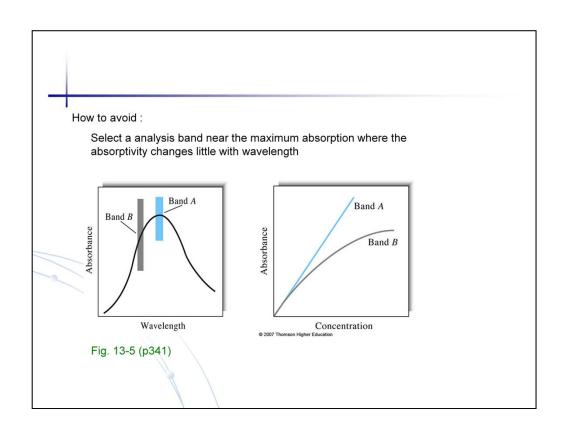


Fig. 7-11 (p176)





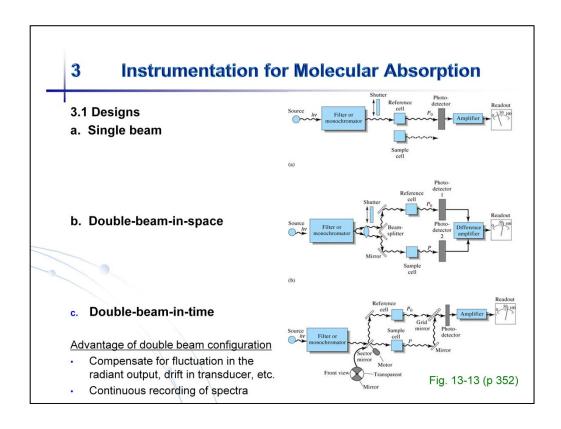
Other physical effects

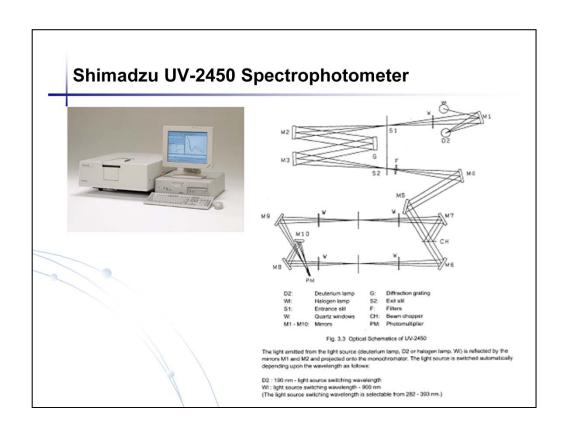
Stray light – scattering, reflection radiation from instrument, outside the nominal wavelength band chosen for measurement

Problem: Stray light hitting the detector will produce erroneous results when the absorbance of a solution is measured, Calculate the apparent absorbance of a solution, if the true absorbance is 0.50 and 3.0% stray light has entered the system (assume the stray light passes through both the sample and the reference cells, without absorption).

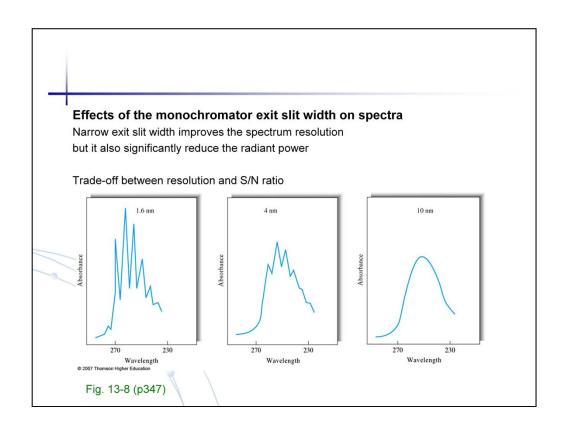
Answer: measured A = 0.47.

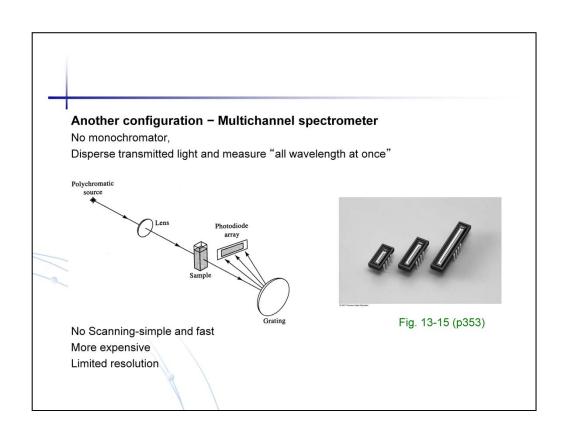
Mismatched cells for the sample and the blank





Wavelength Rai	ge 190 to 900nm (performance guaranteed range). Extendable to 1,100nm through the use of the optional photomultiplier. (The measurable rang maybe restricted in the shorter wavelength side depending on the type of photomultiplier used.)			
Monochromator System	UV-2450: Single monochromator with a high-performance blazed holographic grating in the aberration corrected Czerny-Turner mounting.			
Resolution	0.1nm			
Spectral Bandw	0.1, 0.2, 0.5, 1, 2 and 5nm			
Wavelength Accuracy	±0.3nm			
Wavelength Repeatability	±0.01nm			
Wavelength Scanning Speed	FAST, MEDIUM, SLOW, and SUPER SLOW			
Light Source	50W halogen lamp (2,000 hours of life) and D ² lamp (500 hours of life)			
Light Source lar switching	Selectable between 282nm and 393nm			
Stray Light	UV-2450: Less than 0.015% at 220nm and 340nm			
Detector	Photomultiplier R-928			
Photometric Sys	tem Double beam, direct ratio system with dynode feedback			
Photometric Mo	Absorbance (Abs.), transmittance (%), reflectance (%) and energy (E).			
Photometric Ra	Absorbance: -4~5 Abs. (0.001 Abs. increments) Transmittance: 0~999.9% (0.01 increments) Reflectance: 0~999.9% (0.01 increments)			
Photometric Accuracy	± 0.002 Abs(0~0.5Abs), ± 0.094 Abs(0.5~1Abs), ± 0.3 T (0~100%T) (all determined with NIST 930D standard filter)			
Photometric Repeatability	0.001Abs (0~0.5Abs), ±0.1%T			
Baseline Correct	ion Selectable with storage in firmware			
Baseline Flatnes	Within ± 0.001 Abs. (excluding noise, 2nm slit width and SLOW wavelength scanning speed)			
Drift	Less than 0.0004 Abs. per hour (after 2 hours warm-up)			
Dimensions	570 (W) x 660 (D) x 275 (H) (mm)			
Weight	36kg			
Power Supply	AC 100V/120V/220V/240V, 50/60Hz 250VA (switch-selectable)			





3.2 Noise of spectrophotometric analyses

$$c = -\frac{1}{\varepsilon b} \log T$$

$$\frac{\partial c}{\partial T} = -\frac{0.434}{\varepsilon b T}$$

$$\sigma_c^2 = (\frac{\partial c}{\partial T})^2 \sigma_T^2$$

$$s_c = \sqrt{\sigma_c^2}$$

$$s_T = \sqrt{\sigma_T^2}$$

$$\frac{s_c}{c} = \frac{0.434s_T}{T \log T}$$

Use calculus to show that the minimum uncertainty occurs at 36.8%e, assuming the S_{T} is independent of concentration

Sources of instrumental noise

$${\it Case I} \quad s_{\scriptscriptstyle T} = k_{\scriptscriptstyle 1}$$

Limited readout resol. (3-1/2 digit displays $\rightarrow 0.1\%$ uncertainty from 0% -100% T)

Thermal noise in thermal detector, etc.

$${\rm Case\ II} \quad s_{\scriptscriptstyle T} = k_{\scriptscriptstyle 2} \sqrt{T^{\scriptscriptstyle 2} + T}$$

Shot noise in photon detector (random emission of photon from light source or e- from PMT cathode)

Case III
$$S_T = k_3 T$$

Flicker noise

Fail to position sample and blank cells reproducibly in replicate measurements (as a result, different sections of cell window are exposed to radiation, and reflection/scattering losses change)

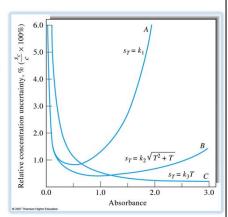


Fig. 13-7 (p345)

Fluorescence and Instrumentation 4

4.1 Fluorescence quantum yield

- ratio of number of molecules fluorescing to number excited

$$\Phi_{fluoro} = \frac{\text{number of photons fluorescing}}{\text{number of molecules excited}}$$

$$= \frac{k_f}{\underbrace{k_f + k_i + k_{ec} + k_{ic} + k_{pd} + k_d}_{\text{rate constants for deactivation processes}}}$$

- $-k_{\it f}, k_{\it pd}$ and $k_{\it d}$ reflects structural effects, the remaining $\it k$'s reflect chemical environments
- -Not all molecules are able to fluoresce

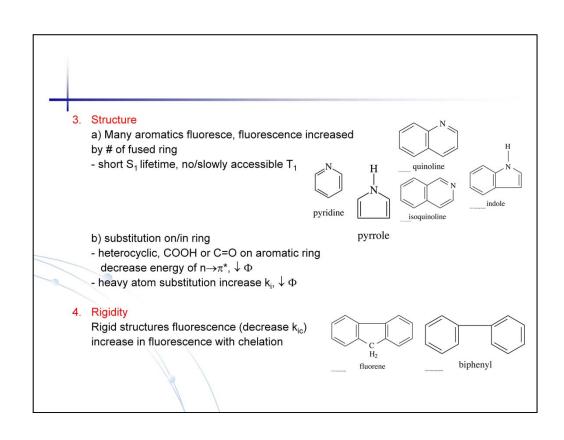
Factors affect Φ_{fluoro}

1. Transition types

Short λ' s $(\sigma^\star\to\sigma)$ break bonds \to increase k_{pd} and k_d , rarely observed. most common emission from $\pi^\star\to\pi$ and $\pi^\star\to n$

2. Lifetime of state

Large fluorescence from high ϵ state/short lifetime/ $\pi \to \pi^*$ (high ϵ , short lifetime 10⁻⁹ -10⁻⁷ s) > n $\to \pi^*$ (low ϵ , long lifetime 10⁻⁷ -10^{-5s}) Large ϵ implies short lifetime, larger k_f



 Temperature, pH, solvent
 ↑ temp, ↑ k_{ec}; ↓ viscosity, ↑ k_{ec};
 pH affects electronic structure of acidic or basic substituents;
 dissolved oxygen (paramagnetic), 1 ki heavy atom effect(solutes and solvent), \(\Lambda \) k_i

6. Concentration

Fluorescence
$$\overrightarrow{F} = K' (P_0 - P) = K' P_0 (1 - 10^{-\frac{A}{\varepsilon b c}})$$

$$= K' P_0 (2.303\varepsilon bc - \frac{(2.303\varepsilon bc)^2}{2!} + \frac{(2.303\varepsilon bc)^3}{3!} + \cdots J \text{ (Maclaurin series)}$$

$$= K' \cdot 2.303\varepsilon bc \cdot P_0 \text{ (when A < 0.05)}$$

$$= K \cdot c$$

- * only works at low A (<0.05), otherwise high-order terms become important
- * self quenching (collision between excited states)
- * secondary absorption (emission reabsorbed by other molecules in solution)

7. Collision quenching (dynamic quenching) - Stern-Volmer equation

$$\Phi_{f}^{0} = \frac{k_{f}}{k_{f} + k_{ec} + k_{ic} + k_{pd} + k_{d}}$$

$$\Phi_f = \frac{k_f}{k_f + k_{ec} + k_{ic} + k_{pd} + k_d + k_q[Q]},$$
 where k_q is the quenching constant and [Q] is the quencher concentration

$$\frac{\Phi_{\rm f}^0}{\Phi_{\rm f}} = 1 + k_d'[Q],$$

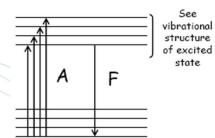
where
$$k_d' = \frac{k_q}{k_f + k_{ec} + k_{ic} + k_{pd} + k_d}$$

$$\frac{F_0}{F} = 1 + k_d'[Q]$$

4.2 Excitation and emission spectra

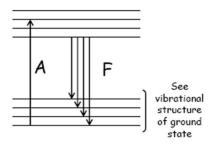
Excitation Spectra

- Excitation at a range of wavelengths
- Emission at a specific (λ_{em})

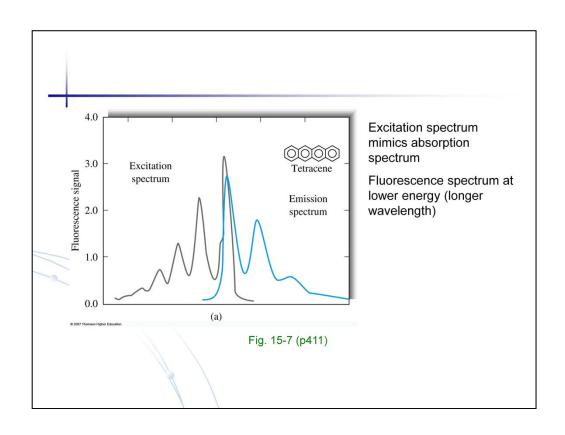


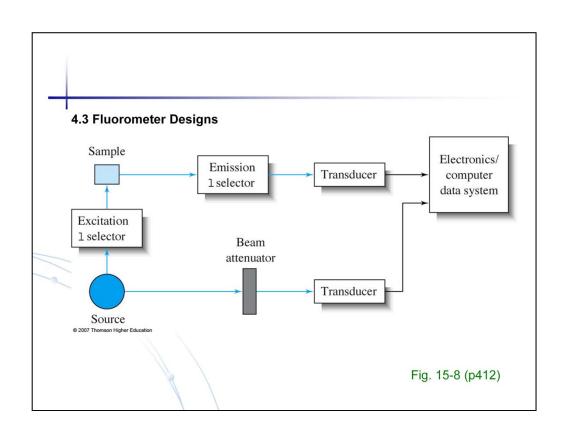
Emission Spectra

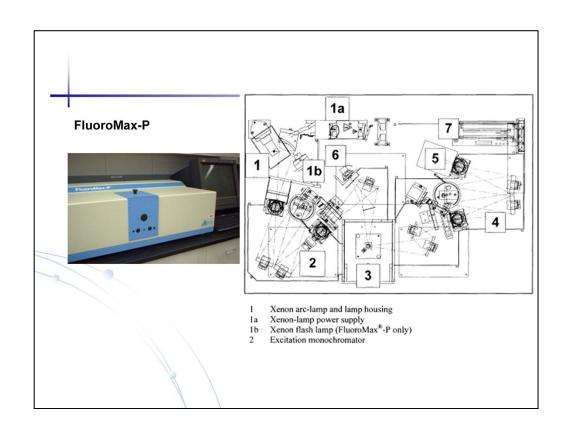
- Excitation at a single wavelength (λ_{ex})
- Emission at a range of wavelengths (long λ)

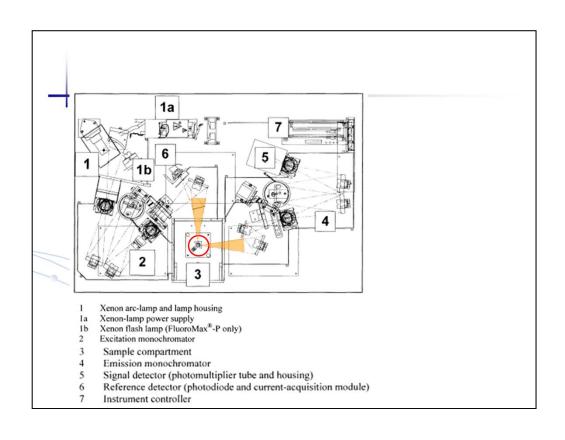


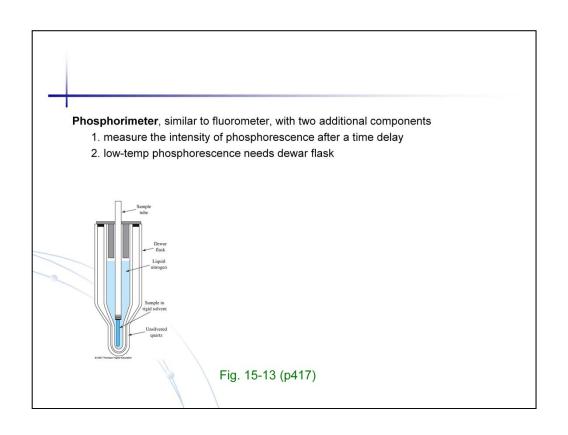
Excitation spectrum should mimic absorption spectrum











4 Applications of Molecular Spectrometry

4.1 Absorption has limited qualitative application

Solvent effects on the UV-Vis spectra Polar solvents "blur" vibrational features Polar solvents shift absorption maxima

 $n\to \pi^\star$

plue sni

 $\pi \to \pi^\star \qquad \qquad \text{red shift}$

UV-Vis not reliable for qualitative but excellent for quantitative analysis

But it is excellent for quantitative analysis

Determining the relationship between \emph{A} and \emph{c}

External Standards

Standard-Addition

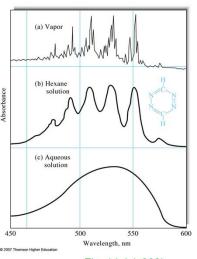
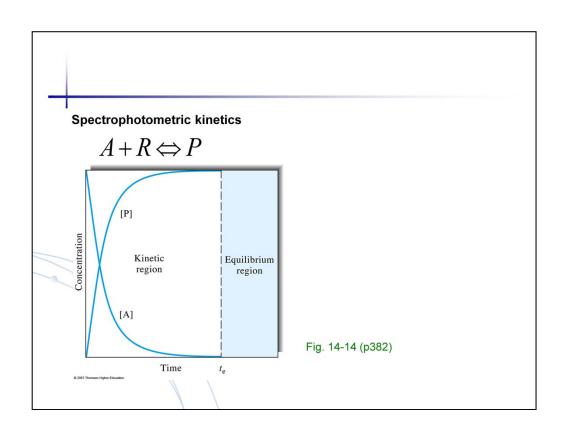
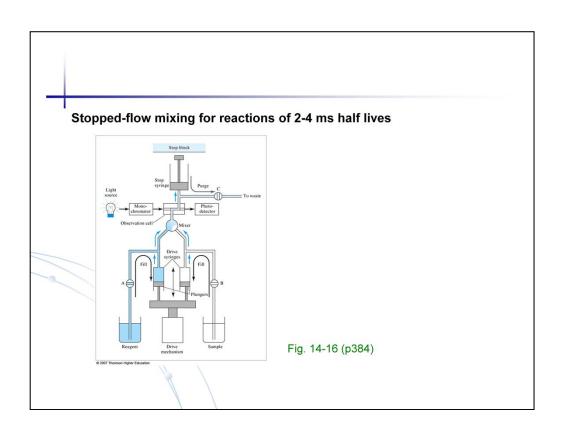


Fig. 14-1 (p368)





4.2 Fluorescence has better sensitivity

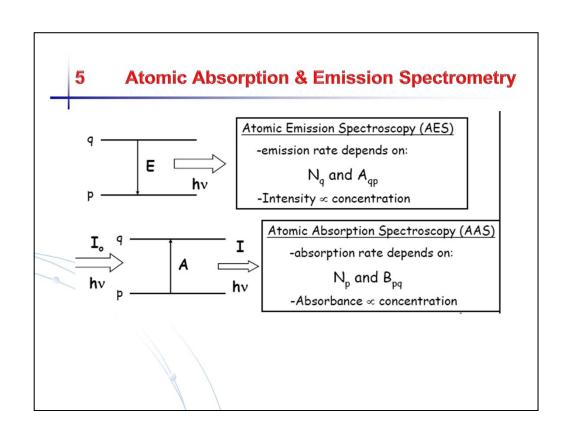
Not universally applicable

Better detection limit (ppb or below) than UV/VIS absorbance

- Nature of emission versus absorbance measurement
- Signal dependence on source intensity

Limited qualitative analysis

Multi-component analysis requires separation (excellent detection method for HPLC compounds that fluoresce)



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5.1 Atomic energy level diagrams

Every element has an unique set of atomic orbitals p, d, f.. split by spin-orbit coupling

Spin (s) and orbital (I) motion create magnetic fields that perturb each other (couple) if fields parallel — higher energy if fields antiparallel — lower energy.

Define spin-orbit coupling by J (total angular momentum)

J = L + S (L=ΣI S= Σs) (positive values only)

Examples:

s electron (I = 0, s = +1/2 or -1/2) J = 0 + ½ = ½

p electron (I = 1, s = +1/2 or -1/2) J = 1+1/2 = 3/2 (higher energy) or

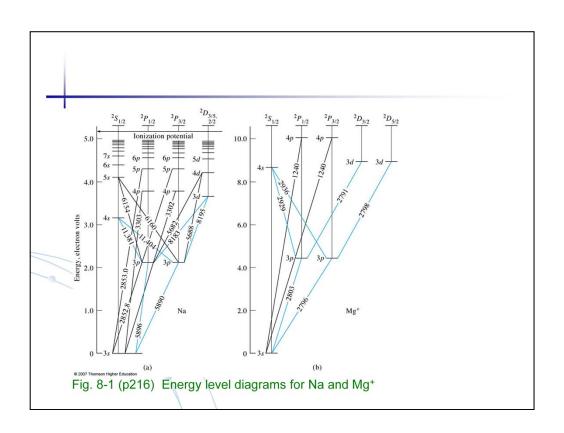
J = 1-1/2 = 1/2 (lower energy)

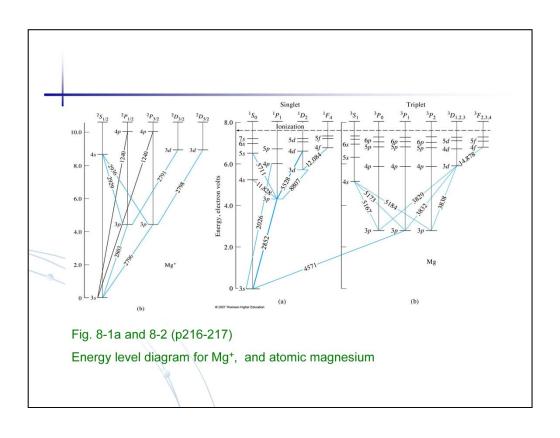
Electronic term symbol

25*1L<sub>J</sub> L written as letter (S, P, D) instead of number

Na = 1s<sup>2</sup>2s<sup>2</sup>2p<sup>6</sup>3s<sup>1</sup>, L = 0, S= 1/2, <sup>2</sup>S<sub>1/2</sub>

Na* = 1s<sup>2</sup>2s<sup>1</sup>2p<sup>6</sup>3p<sup>1</sup>, L = 1, S= 1/2, <sup>2</sup>P<sub>3/2, 1/2</sub>
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- Similar pattern between atoms but different spacing
- Spectrum of an ion different to that of the corresponding atom
- Energy levels measured in electron volts (eV) 1 eV = $1.602 \times 10^{-19} \text{ C} \times 1 \text{ V}(\text{J/C}) = 1.602 \times 10^{-19} \text{ J}$ = $96.484 \text{ kJ .mol}^{-1}$
- As number of electron increases, the number of levels increases, emission spectra become more complex

5.2 Atomic line widths

5.2.1 Line broadening from the uncertainty principle

Uncertainty principle: must measure for some minimum time to tell two frequencies apart

 $\Delta t \cdot \Delta E \ge h$

 $\Delta t \cdot \Delta \nu \ge 1$

 Δt : minimum time for measurement

 $\Delta\nu\textsubscript{:}$ minimum detectable difference in frequencies

Shows up in lifetime of excited state

- if lifetime infinitely long, ∆E infinitely narrow
- if lifetime short, ΔE is broadened

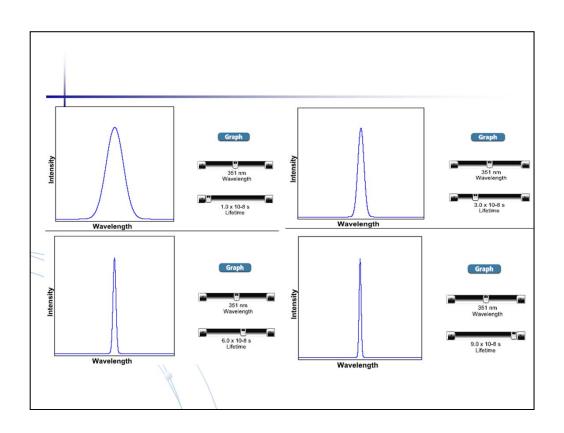
 $v = c/\lambda$

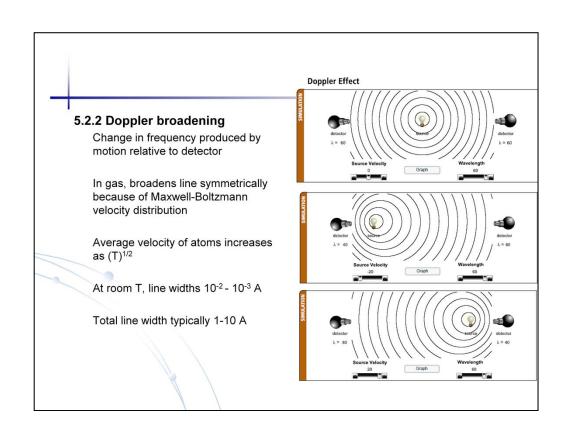
Differentiating $\,\nu$ with regard to $\,\lambda$

 $dv = -c\lambda^2 d\lambda, \ dv \approx \Delta v \ and \ d\lambda \approx \Delta \lambda$

 $\Delta \lambda = \Delta v \lambda^2 / c$

natural line widths





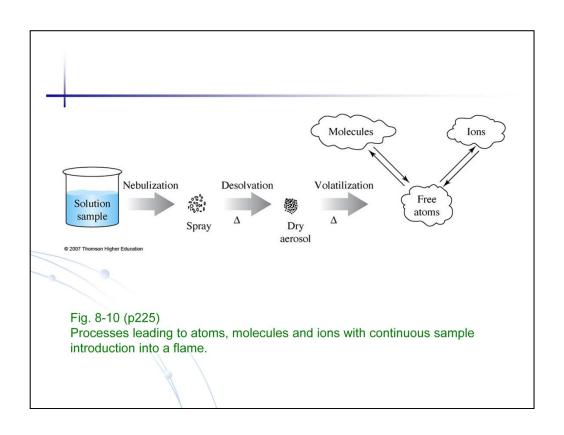
5.2.3 Pressure broadening Collisions with other atoms transfer small quantities of energy (heat) – ill-defined ground state energy Effects worse at high pressures - for low pressure hollow cathode lamp (1-10 torr) 10-1 -10-2 A - for high pressure Xeon lamps (>10,000 torr) 100-1000 A (continuum radiation!)

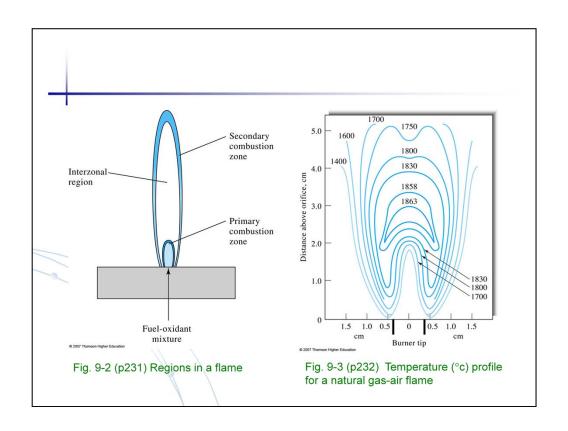
5.3 AAS

- determination of elements not compounds
- · needs radiation source
- high temperature for atomization

5.3.1 Atomization

- Flame atomizer for solutions
- 1. Desolvation: solvent evaporates to produce solid aerosol
- 2. Volatilization: form the gas molecules
- 3. Dissociation: produce atomic gas
- 4. {lonization: ionize to form cations + electrons}
- 5. {Excitation: excited by heat of flame, emission}





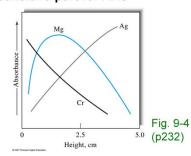
Flame structure

- a. Primary combustion zone:
 blue luminescence from emission of C₂/CH
 cool {thermal equilibrium not achieved}
 initial decomposition, molecular fragments
- b. Interzonal region: hottest (several cm) most free atoms, wildly used part
- c. Secondary combustion zone:
 cooler
 conversion of atoms to molecular oxides
 {then disperse to surroundings}

Flame temperatures

Fuel	Oxidant	T (°C)
Natural gas	Air	1700 ~ 1900
H_2	O_2	2550 ~ 2700
Acetylene	O_2	3050 ~ 3000

Sensitive part for AAS



- Sensitivity varies with element Element rapidly oxides – near burner Element poorly oxidizes – away from burner
- Optimize burner position for each element
 - Difficult for multi-element detection

Laminar flow burner

- · Stable and quite flame
- Long path length for absorption
- Disadvantages: short residence time in the flame (0.1 ms)

low sensitivity (a large fraction of sample flows down the drain)

Flashback

Advantages

- Simplest atomization, needs preliminary sample treatment.
- Best for reproducibility (relative error <1%)
- Relatively intensive incomplete volatilization, short time in beam

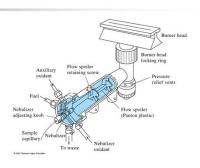


Fig. 9-5 (p233) A laminar-flow burner

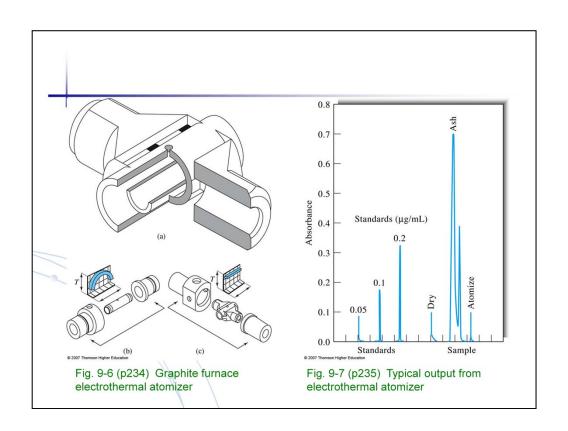
- Electrothermal atomization (Method of choice when flame atomization fails)
- Analysis of solutions as well as solids
- Three stages: dry at low temperature (120°C, 20s)
 - ash at higher temperature(500-1000°C, 60s), removal of volatile hydroxides, sulfates, carbonates
 - atomize of remaining analyte at 2000-3000 °C (ms~s)
- High sensitivity ← less sample and longer residence time in optical path (10⁻¹⁰ -10⁻¹³ g analyte, 0.5-10uL sample, 2x10⁻⁶ -1x10⁻⁵ ppm)
- Less reproducible (relative precision 5-10%)
- · Slow (several minutes for each element)
- Narrow dynamic range

Two inert gas stream are provided

- External Ar gas prevents outside air from entering/incinerating tube
- · Internal Ar gas circulate the gaseous analyte

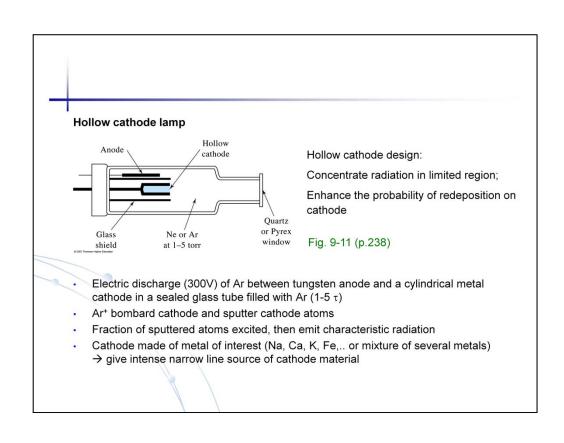
Output signals from graphite furnace

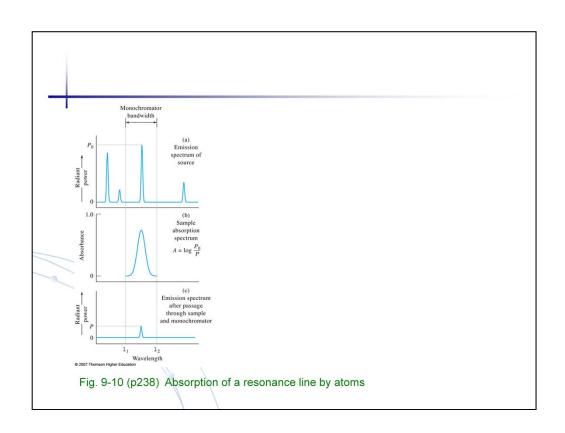
- Drying
- · Ashing (both from volatile absorbing species, smoke scattering)
- Atomize (used for analysis)

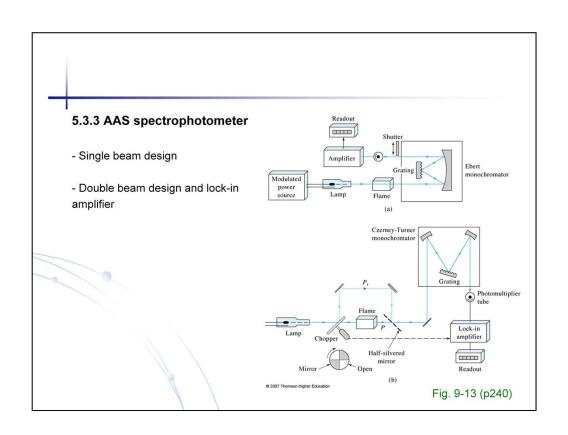


5.3.2 Radiation source

- Each element has narrow absorption lines (0.002-0.005nm), very selective.
- For a linear calibration curve (Beer's law), source bandwidth should be narrower than the width of an absorption line.
 - continuum radiation source requests a monochromator with $\Delta\lambda_{\text{eff}}$ < 10-4 nm, difficult!
- Solutions:
 - LINE source at discrete wavelength,
 resonance line, using 589.6 nm emission line of sodium as a source to probe Na in
 analyte
 - operate line source with bandwidth narrower than the absorption line width minimize the Doppler broadening lower temperature and pressure than atomizer







5.4 AES

Sample introduction

- 1. Nebulizer convert solutions to fine spray or aerosol
- 2. Electrothermal vaporizer (ETV)

Only for introduction, not atomization

3. Other methods

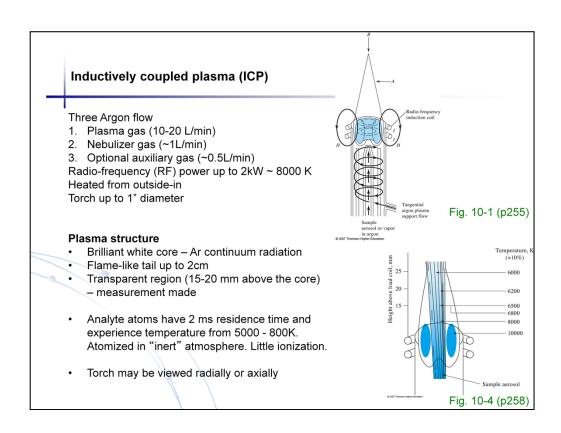
Direct insertion {powder placed inside flame, plasma, arc or spark atomizer} Laser ablation {uses laser to vaporize sample}

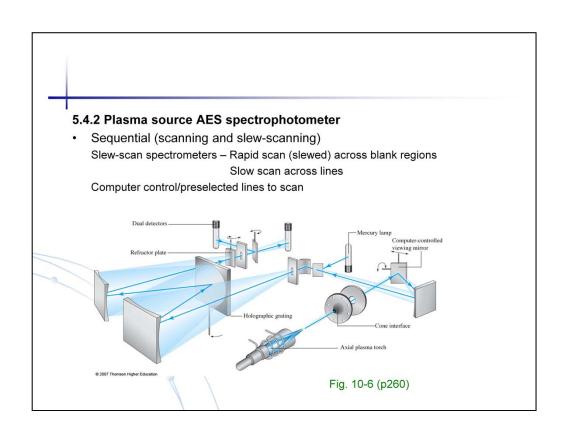
5.4.1 Atomization for AES

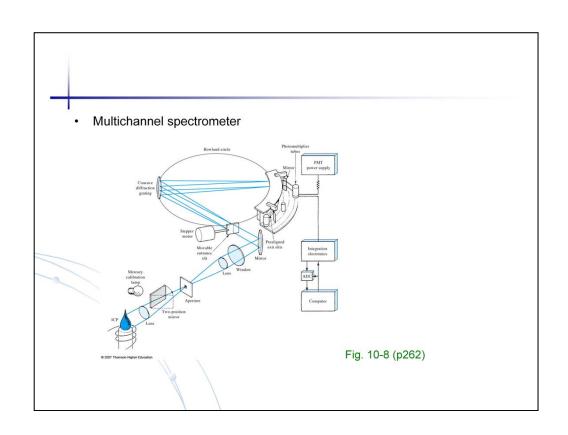
$$\frac{N_j}{N_0} = \frac{g_j}{g_0} \exp(-\frac{E_j}{kT})$$

Emission relies on the number of excited atoms, requiring close control of temperature (e.g., at 2500K Na only has 0.02% atoms in the 1st excited state, a rise of 10 K in temperature results in 4% increase of excited atoms)

Less important in absorption, 99.8% atoms in ground state!







5.5 Plasma AES vs. Flame AAS

AAS

Similar atomization technique to AES
Addition of radiation source
High temperature for atomization
(flame and electrothermal atomization)
Low cost instrumentation
Single element
Quantitative
Low sample throughput
Atomization interference
Detection limit 0.001-0.020 ppm
Greater precision

complementary techniques

AES

No radiation source Very high temperature for excitation (plasma/arc/spark) moderate-high cost simultaneous multielement analysis qualitative and quantitative high sample throughput spectral interference (large # of lines) 10ppb